## Mathematical properties of an integro-differential model from population genetics

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## Résumé

The model describes the dynamics of fitness distribution in an asexual population under the effect of mutation and selection. These two processes are represented by two nonlocal terms. First, we prove the existence and uniqueness of the solution, and we derive asymptotic estimates of the distribution as the fitness tends to infinity. Based on these asymptotic estimates, we then show that the cumulant generating function of the distribution is welldefined and satisfies a linear nonlocal transport equation that we solve explicitly. This explicit formula allows us to characterize the dependence of the long time behavior of the distribution with respect to the mutation kernel. On the one hand, if the kernel contains some beneficial mutations, the distribution diverges, which is reminiscent of the results of [Alfaro and Carles, 2014] who analysed a mutator-replicator equation with a diffusive mutation term. On the other hand, if the initial fitness distribution admits some upper bound, purely deleterious kernels lead to the convergence of the distribution towards an equilibrium. The shape of the equilibrium distribution strongly depends on the kernel through its harmonic mean : the distribution admits a positive mass at the best initial fitness class if and only if the harmonic mean is non zero. The talk is based on a joint work with François Hamel (I2M, AMU), Guillaume Martin (ISEM, CNRS) and Lionel Roques (BioSP, INRA).

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